

# Pre-Calculus (AP / ACC) Summer Prep Packet

Welcome to Pre-Calculus! This packet is for all students entering AP Pre-Calculus or Accelerated Pre-Calculus.

Attached, you will find the basic learning targets from Algebra and Geometry that you are expected to remember **BEFORE** you come to class in the fall. For each topic addressed, this packet contains review examples, properties, definitions, and online video tutorial links followed by practice problems. This material must be mastered in order for you to be successful in Pre-Calculus. You will be assessed at the beginning of the school year. Since this material is designed as a review, you are responsible for completing this packet on your own. The packet will be graded to assess the student's **EFFORTS** to recall this information. Be sure to **show your work!**

Name: \_\_\_\_\_

# Target Checklist

## **Target 1: Radicals**

- ☐ A. Simplify
- ☐ B. Rationalize
- ☐ Complex Numbers

## **Target 2: Geometry**

- ☐ A. Pythagorean Theorem
- ☐ B. Special Right Triangles

## **Target 3: Equations and Graphing**

- ☐ A. Writing Equations of a Line
- ☐ B. Graphing Equations and Inequalities

## **Target 4: Systems of Equations**

- ☐ A. Substitution
- ☐ B. Elimination

## **Target 5: Exponents**

## **Target 6: Polynomials and Quadratics**

- ☐ A. Simplify Expressions
- ☐ B. Multiply
- ☐ C. Factoring
- ☐ D. Solving Quadratic Equations
- ☐ E. Discriminant
- ☐ F. Quadratic Formula
- ☐ G. Division

## **Target 7: Functions**

- ☐ A. Evaluate
- ☐ B. Compositions and Inverses

## **Target 8: Radical Expressions and Equations**

- ☐ A. Multiply and Divide Rational Expressions
- ☐ B. Add and Subtract Rational Expressions
- ☐ C. Complex Fractions
- ☐ D. Solve Rational Equations

## Target 1:

### Summer Review Packet for Students Entering Pre-Calculus

#### Radicals:

To simplify means that 1) no radicand has a perfect square factor and  
2) there is no radical in the denominator (rationalize).

Recall – the **Product Property**  $\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$  and the **Quotient Property**  $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$

**Examples:** Simplify  $\sqrt{24} = \sqrt{4} \cdot \sqrt{6}$  find a perfect square factor  
 $= 2\sqrt{6}$  simplify

Simplify  $\sqrt{\frac{7}{2}} = \frac{\sqrt{7}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$  split apart, then multiply by both the numerator and the  
denominator by  $\sqrt{2}$   
 $= \frac{\sqrt{14}}{\sqrt{4}} = \frac{\sqrt{14}}{2}$  multiply straight across and simplify

If the denominator contains 2 terms –

multiply the numerator and the denominator by the *conjugate* of the denominator

The **conjugate** of  $3 + \sqrt{2}$  is  $3 - \sqrt{2}$  (the sign changes between the terms).

Simplify each of the following:

1.  $\sqrt{32}$

2.  $\sqrt{(2x)^8}$

3.  $\sqrt[3]{-64}$

4.  $\sqrt{49m^2n^8}$

5.  $\sqrt{\frac{11}{9}}$

6.  $\sqrt{60} \cdot \sqrt{105}$

7.  $(\sqrt{5} - \sqrt{6})(\sqrt{5} + \sqrt{6})$

Rationalize.

8.  $\frac{1}{\sqrt{2}}$

9.  $\frac{2}{\sqrt{3}}$

10.  $\frac{3}{2-\sqrt{5}}$

## Complex Numbers:

Form of complex number -  $a + bi$

Where  $a$  is the “real” part and  $bi$  is the “imaginary” part

Always make these substitutions  $\sqrt{-1} = i$  and  $i^2 = -1$

- To simplify: pull out the  $\sqrt{-1}$  before performing any operation

**Example:**  $\sqrt{-5} = \sqrt{-1} \cdot \sqrt{5}$  Pull out  $\sqrt{-1}$   
 $= i\sqrt{5}$  Make substitution

**Example:**  $(i\sqrt{5})^2 = i\sqrt{5} \cdot i\sqrt{5}$  List twice  
 $= i^2 \sqrt{25}$  Simplify  
 $= (-1)(5) = -5$  Substitute

- Treat  $i$  like any other variable when  $+$ ,  $-$ ,  $\times$ , or  $\div$  (but always simplify  $i^2 = -1$ )

**Example:**  $2i(3 + i) = 2(3i) + 2i(i)$  Distribute  
 $= 6i + 2i^2$  Simplify  
 $= 6i + 2(-1)$  Make substitution  
 $= -2 + 6i$  Simplify and rewrite in complex form

- Since  $i = \sqrt{-1}$ , no answer can have an ‘ $i$ ’ in the denominator **RATIONALIZE!!**

**Simplify.**

9.  $\sqrt{-49}$

10.  $6\sqrt{-12}$

11.  $-6(2 - 8i) + 3(5 + 7i)$

12.  $(3 - 4i)^2$

13.  $(6 - 4i)(6 + 4i)$

**Rationalize.**

14.  $\frac{1 + 6i}{5i}$



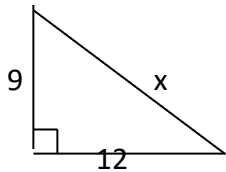
## Target 2:

### Geometry:

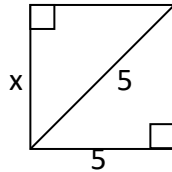
Pythagorean Theorem (right triangles):  $a^2 + b^2 = c^2$

Find the value of  $x$ .

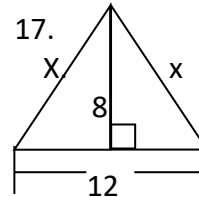
15.



16.

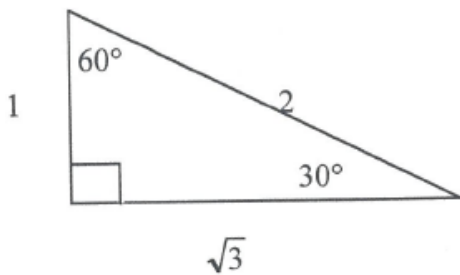


17.

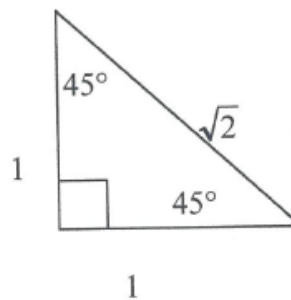


18. A square has perimeter 12 cm. Find the length of the diagonal.

\* In  $30^\circ - 60^\circ - 90^\circ$  triangles, sides are in proportion  $1, \sqrt{3}, 2$ .

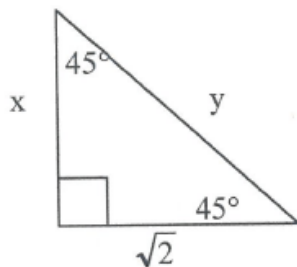


\* In  $45^\circ - 45^\circ - 90^\circ$  triangles, sides are in proportion  $1, 1, \sqrt{2}$ .

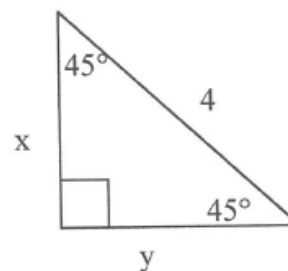


Solve for  $x$  and  $y$ .

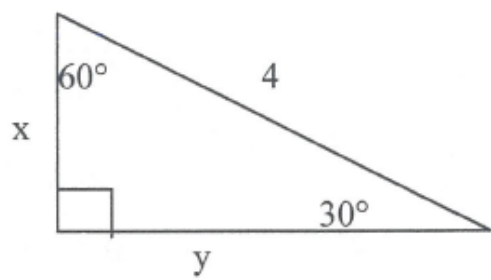
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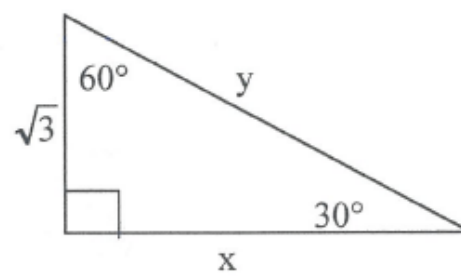
20.



21.



22.



## Target 3:

### Equations of Lines:

**Slope intercept form:**  $y = mx + b$

**Vertical line:**  $x = c$  (slope is undefined)

**Point-slope form:**  $y - y_1 = m(x - x_1)$

**Horizontal line:**  $y = c$  (slope is 0)

**Standard Form:**  $Ax + By = C$

**Slope:**  $m = \frac{y_2 - y_1}{x_2 - x_1}$

23. State the slope and y-intercept of the linear equation:  $5x - 4y = 8$ .

24. Find the x-intercept and y-intercept of the equation:  $2x - y = 5$

25. Write the equation in standard form:  $y = 7x - 5$

**Write the equation of the line in slope-intercept form with the following conditions:**

26. slope = -5 and passes through the point (-3, -8)

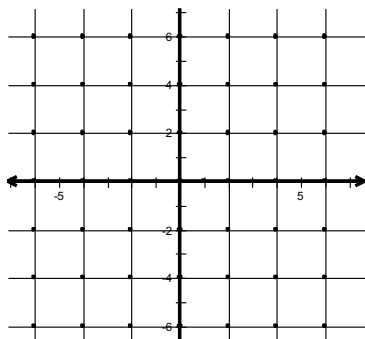
27. passes through the points (4, 3) and (7, -2)

28. x-intercept = 3 and y-intercept = 2

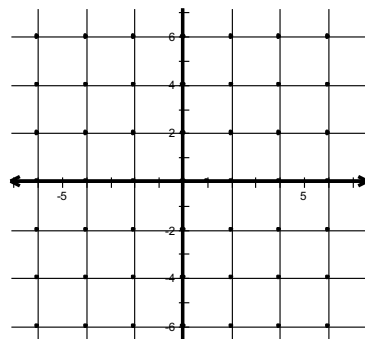
## Graphing:

Graph each function, inequality, and / or system.

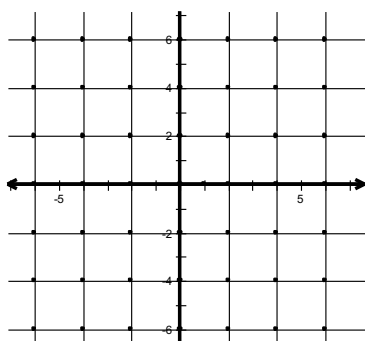
29.  $3x - 4y = 12$



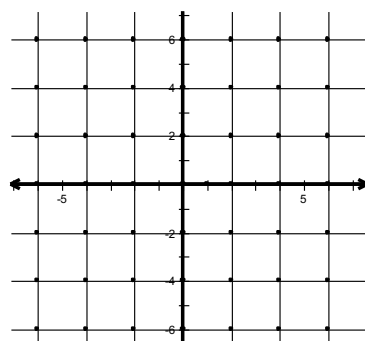
30. 
$$\begin{cases} 2x + y = 4 \\ x - y = 2 \end{cases}$$



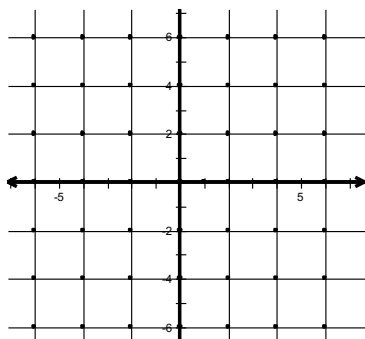
31.  $y < -4x - 2$



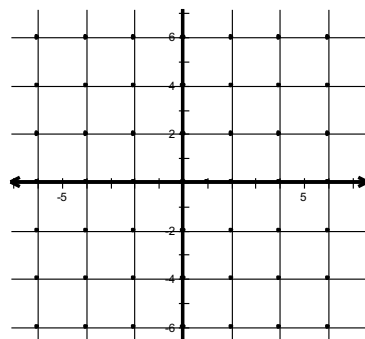
32.  $y + 2 = |x + 1|$



33.  $y > |x| - 1$



34.  $y + 4 = (x - 1)^2$



Vertex: \_\_\_\_\_

x-intercept(s): \_\_\_\_\_

y-intercept(s): \_\_\_\_\_

## Target 4:

### Systems of Equations:

$$3x + y = 6$$

$$2x - 2y = 4$$

#### Substitution:

Solve 1 equation for 1 variable.

Rearrange.

Plug into 2<sup>nd</sup> equation.

Solve for the other variable.

Then plug answer back into an original equation to solve for the 2<sup>nd</sup> variable.

$$y = 6 - 3x \quad \text{solve 1<sup>st</sup> equation for y}$$

$$2x - 2(6 - 3x) = 4 \quad \text{plug into 2<sup>nd</sup> equation}$$

$$2x - 12 + 6x = 4 \quad \text{distribute}$$

$$8x = 16 \quad \text{simplify}$$

$$x = 2$$

Plug  $x = 2$  back into original

$$3(2) + y = 6$$

$$6 + y = 6$$

$$y = 0$$

#### Elimination:

Find opposite coefficients for 1 variable.

Multiply equation(s) by constant(s).

Add equations together (lose 1 variable).

Solve for variable.

Solve for variable.

$$6x + 2y = 12 \quad \text{multiply 1<sup>st</sup> equation by 2}$$

$$2x - 2y = 4 \quad \text{coefficients of y are opposite}$$

$$8x = 16 \quad \text{add}$$

$$x = 2 \quad \text{simplify}$$

Solve each system of equations. Use any method. (Answers may NOT be whole numbers.)

$$35. \begin{cases} 2x + y = 4 \\ 3x + 2y = 1 \end{cases}$$

$$36. \begin{cases} 2x + y = 4 \\ 3x - y = 14 \end{cases}$$

$$37. \begin{cases} 2w - 5z = 13 \\ 6w + 3z = 10 \end{cases}$$

## Target 5:

### Exponents:

#### TWO RULES OF ONE

1.  $a^1 = a$

*Any number raised to the power of one equals itself.*

2.  $1^a = 1$

*One to any power is one.*

#### ZERO RULE

3.  $a^0 = 1$

*Any nonzero number raised to the power of zero is one.*

#### PRODUCT RULE

4.  $a^m \cdot a^n = a^{m+n}$

*When multiplying two powers that have the same base, add the exponents.*

#### QUOTIENT RULE

5.  $\frac{a^m}{a^n} = a^{m-n}$

*When dividing two powers with the same base, subtract the exponents.*

#### POWER RULE

6.  $(a^m)^n = a^{m \cdot n}$

*When a power is raised to another power, multiply the exponents.*

#### NEGATIVE EXPONENTS

7.  $a^{-n} = \frac{1}{a^n}$  and  $\frac{1}{a^{-n}} = a^n$

*Any nonzero number raised to a negative power equals its reciprocal raised to the opposite positive power.*

Express each of the following in simplest form. Answers should not have any negative exponents.

38.  $5a^0$

39.  $\frac{3c}{c^{-1}}$

40.  $\frac{2ef^{-1}}{e^{-1}}$

41.  $\frac{(n^3 p^{-1})^2}{(np)^{-2}}$

Simplify.

42.  $3m^2 \cdot 2m$

43.  $(a^3)^2$

44.  $(-b^3 c^4)^5$

45.  $4m(3a^2 m)$

## Target 6:

### Polynomials and Quadratics:

To add / subtract polynomials, combine like terms.

EX:  $8x - 3y + 6 - (6y + 4x - 9)$  *Distribute the negative through the parantheses.*  
 $= 8x - 3y + 6 - 6y - 4x + 9$  *Combine terms with similar variables.*  
 $= 8x - 4x - 3y - 6y + 6 + 9$   
 $= 4x - 9y + 15$

**Simplify.**

48.  $3x^3 + 9 + 7x^2 - x^3$

49.  $7m - 6 - (2m + 5)$

To multiplying two binomials, use **FOIL**.

EX:  $(3x - 2)(x + 4)$  *Multiply the first, outer, inner, then last terms.*  
 $= 3x^2 + 12x - 2x - 8$  *Combine like terms.*  
 $= 3x^2 + 10x - 8$

**Multiply.**

48.  $(3a + 1)(a - 2)$

49.  $(s + 3)(s - 3)$

50.  $(c - 5)^2$

51.  $(5x + 7y)(5x - 7y)$

**Factoring.**

Follow these steps in order to factor polynomials.

**STEP 1:** Look for a GCF in ALL of the terms.

- a.) If you have one (other than 1) factor it out front.
- b.) If you don't have one, move on to STEP 2.

**STEP 2:** How many terms does the polynomial have?

**2 Terms**

- a.) Is it difference of two squares?  $a^2 - b^2 = (a + b)(a - b)$

**EX:**  $x^2 - 25 = (x + 5)(x - 5)$

- b.) Is it sum or difference of two cubes?

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

**EX:**  $m^3 + 64 = (m + 4)(m^2 - 4m + 16)$

$$p^3 - 125 = (p - 5)(p^2 + 5p + 25)$$

**3 Terms**

$$x^2 + bx + c = (x + \quad)(x + \quad)$$

**Ex:**  $x^2 + 7x + 12 = (x + 3)(x + 4)$

$$x^2 - bx + c = (x - \quad)(x - \quad)$$

$$x^2 - 5x + 4 = (x - 1)(x - 4)$$

$$x^2 + bx - c = (x - \quad)(x + \quad)$$

$$x^2 + 6x - 16 = (x - 2)(x + 8)$$

$$x^2 - bx - c = (x - \quad)(x + \quad)$$

$$x^2 - 2x - 24 = (x - 6)(x + 4)$$

**4 Terms** -- Factor by Grouping

- a.) Pair up first two terms and last two terms
- b.) Factor out GCF of each pair of numbers.
- c.) Factor out front the parentheses that the terms have in common.
- d.) Put leftover terms in parentheses.

$$\begin{aligned} \text{Ex: } x^3 + 3x^2 + 9x + 27 &= (x^3 + 3x^2) + (9x + 27) \\ &= x^2(x + 3) + 9(x + 3) \\ &= (x + 3)(x^2 + 9) \end{aligned}$$

**Factor Completely.**

52.  $z^2 + 4z - 12$

53.  $6 - 5x - x^2$

54.  $2k^2 + 2k - 60$



55.  $-10b^4 - 15b^2$

56.  $9c^2 + 30c + 25$

57.  $9n^2 - 4$

58.  $27z^3 - 8$

59.  $2mn - 2mt + 2sn - 2st$

**To solve quadratic equations, try to factor first and set each factor equal to zero. Solve for your variable. If the quadratic does NOT factor, use quadratic formula.**

**EX:**  $x^2 - 4x = 21$       *Set equal to zero FIRST.*

$x^2 - 4x - 21 = 0$       *Now factor.*

$(x + 3)(x - 7) = 0$       *Set each factor equal to zero.*

$x + 3 = 0$      $x - 7 = 0$       *Solve each for x.*

$x = -3$        $x = 7$

**Solve each equation.**

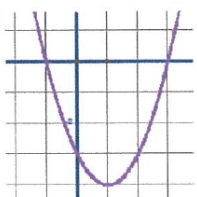
60.  $x^2 - 4x - 12 = 0$

61.  $x^2 + 25 = 10x$

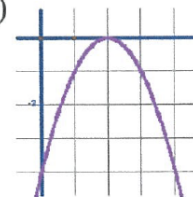
62.  $x^2 - 14x + 19 = 0$

**DISCRIMINANT:** The number under the radical in the quadratic formula ( $b^2 - 4ac$ ) can tell you what kinds of roots you will have.

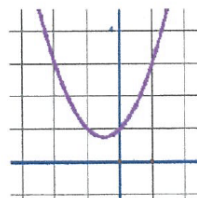
**IF**  $b^2 - 4ac > 0$  **you will have TWO real roots.**  
(touches x-axis twice)



**IF**  $b^2 - 4ac = 0$  **you will have ONE real root**  
(touches the x-axis once)



**IF**  $b^2 - 4ac < 0$  **you will have TWO imaginary roots.**  
(Graph does not cross the x-axis)



**QUADRATIC FORMULA** – allows you to solve any quadratic for all its real and imaginary

roots.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

**EX:** In the equation:  $x^2 + 2x + 3 = 0$ , find the value of the discriminant, describe the nature of the roots, then solve.

$$x^2 + 2x + 3 = 0 \quad \text{Determine values for a, b, and c.}$$

$$a = 1 \quad b = 2 \quad c = 3 \quad \text{Find discriminant.}$$

$$D = 2^2 - 4 \cdot 1 \cdot 3$$

$$D = 4 - 12$$

$$D = -8 \quad \text{There are two imaginary roots.}$$

$$\text{Solve: } x = \frac{-2 \pm \sqrt{-8}}{2}$$

$$x = \frac{-2 \pm 2i\sqrt{2}}{2}$$

$$x = -1 \pm i\sqrt{2}$$

Find the value of the discriminant, describe the nature of the roots, then solve each quadratic. Use EXACT values.

63.  $x^2 - 9x + 14 = 0$

64.  $5x^2 - 2x + 4 = 0$

Discriminant = \_\_\_\_\_

Discriminant = \_\_\_\_\_

Types of Roots: \_\_\_\_\_

Types of Roots: \_\_\_\_\_

Roots = \_\_\_\_\_

Roots = \_\_\_\_\_

**Long Division** – can be used when dividing any polynomials.

**Synthetic Division** – can ONLY be used when dividing a polynomial by a linear (degree one) polynomial.

EX: 
$$\frac{2x^3 + 3x^2 - 6x + 10}{x + 3}$$

**Long Division**

$$\begin{array}{r} 2x^3 + 3x^2 - 6x + 10 \\ x + 3 \overline{) 2x^3 + 3x^2 - 6x + 10} \\ \underline{2x^3 - 3x + 3 + \frac{1}{x+3}} \\ = x + 3 \overline{) 2x^3 + 3x^2 - 6x + 10} \\ \underline{(-) (2x^3 + 6x^2)} \\ -3x^2 - 6x \\ \underline{(-) (-3x^2 - 9x)} \\ 3x + 10 \\ \underline{(-) (3x + 9)} \\ 1 \end{array}$$

**Synthetic Division**

$$\begin{array}{r} 2x^3 + 3x^2 - 6x + 10 \\ x + 3 \overline{) 2x^3 + 3x^2 - 6x + 10} \\ -3 \overline{) 2 \quad 3 \quad -6 \quad 10} \\ \downarrow \quad -6 \quad 9 \quad -9 \\ \hline 2 \quad -3 \quad 3 \quad 1 \\ = 2x - 3x + 3 + \frac{1}{x+3} \end{array}$$

Divide each polynomial using long division OR synthetic division.

65. 
$$\frac{c^3 - 3c^2 + 18c - 16}{c^2 + 3c - 2}$$

66. 
$$\frac{x^4 - 2x^2 - x + 2}{x + 2}$$

## Target 7:

**To evaluate a function for a given value, simply plug the value into the function for x.**

Evaluate each function for the given value.

67.  $f(x) = x^2 - 6x + 2$

$f(3) = \underline{\hspace{2cm}}$

68.  $g(x) = 6x - 7$

$g(x+h) = \underline{\hspace{2cm}}$

69.  $f(x) = 3x^2 - 4$

$5[f(x+2)] = \underline{\hspace{2cm}}$

### **Composition and Inverses of Functions:**

**Recall:**  $(f \circ g)(x) = f(g(x))$  OR  $f[g(x)]$  read “*f* of *g* of *x*” Means to plug the inside function (in this case  $g(x)$ ) in for  $x$  in the outside function (in this case,  $f(x)$ ).

**Example:** Given  $f(x) = 2x^2 + 1$  and  $g(x) = x - 4$  find  $f(g(x))$ .

$$\begin{aligned} f(g(x)) &= f(x - 4) \\ &= 2(x - 4)^2 + 1 \\ &= 2(x^2 - 8x + 16) + 1 \\ &= 2x^2 - 16x + 32 + 1 \\ f(g(x)) &= 2x^2 - 16x + 33 \end{aligned}$$

**Suppose**  $f(x) = 2x$ ,  $g(x) = 3x - 2$ , and  $h(x) = x^2 - 4$  . **Find the following:**

70.  $f[g(2)] = \underline{\hspace{2cm}}$

71.  $f[g(x)] = \underline{\hspace{2cm}}$

72.  $f[h(3)] = \underline{\hspace{2cm}}$

73.  $g[f(x)] = \underline{\hspace{2cm}}$

To find the inverse of a function, simply switch the x and the y and solve for the new “y” value.

**Example:**

$f(x) = \sqrt[3]{x+1}$	Rewrite f(x) as y
$y = \sqrt[3]{x+1}$	Switch x and y
$x = \sqrt[3]{y+1}$	Solve for your new y
$(x)^3 = (\sqrt[3]{y+1})^3$	Cube both sides
$x^3 = y+1$	Simplify
$y = x^3 - 1$	Solve for y
$f^{-1}(x) = x^3 - 1$	Rewrite in inverse notation

Find the inverse,  $f^{-1}(x)$ , if possible.

74.  $f(x) = 5x + 2$

75.  $f(x) = \frac{1}{2}x - \frac{1}{3}$

## Target 8:

### **Rational Algebraic Expressions:**

#### **Multiplying and Dividing.**

Factor numerator and denominator completely. Cancel any common factors in the top and bottom. If dividing, change divide to multiply and flip the second fraction.

EX:

$$\frac{x^2 + 10x + 21}{5 - 4x - x^2} \cdot \frac{x^2 + 2x - 15}{x^3 + 4x^2 - 21x} \quad \text{Factor everything completely.}$$

$$= \frac{(x+7)(x+3)}{(5+x)(1-x)} \cdot \frac{(x+5)(x-3)}{x(x-3)(x+7)} \quad \text{Cancel out common factors in the top and bottom.}$$

$$= \frac{(x+3)}{x(1-x)} \quad \text{Simplify.}$$

**Simplify.**

$$76. \frac{5z^3 + z^2 - z}{3z}$$

$$77. \frac{m^2 - 25}{m^2 + 5m}$$

$$78. \frac{10r^5}{21s^2} \cdot \frac{3s}{5r^3}$$

$$79. \frac{a^2 - 5a + 6}{a + 4} \cdot \frac{3a + 12}{a - 2}$$

$$80. \frac{6d - 9}{5d + 1} \div \frac{6 - 13d + 6d^2}{15d^2 - 7d - 2}$$

### Addition and Subtraction.

First, find the least common denominator.

Write each fraction with the LCD.

Add / subtract numerators as indicated and leave the denominators as they are.

$$\text{EX: } \frac{3x+1}{x^2+2x} + \frac{5x-4}{2x+4}$$

*Factor denominator completely.*

$$= \frac{3x+1}{x(x+2)} + \frac{5x-4}{2(x+2)}$$

*Find LCD  $(2x)(x+2)$*

$$= \frac{2(3x+1)}{2x(x+2)} + \frac{x(5x-4)}{2x(x+2)}$$

*Rewrite each fraction with the LCD as the denominator.*

$$= \frac{6x+2+5x^2-4x}{2x(x+2)}$$

*Write as one fraction.*

$$= \frac{5x^2+2x+2}{2x(x+2)}$$

*Combine like terms.*

81.  $\frac{2x}{5} - \frac{x}{3}$

82.  $\frac{b-a}{a^2b} + \frac{a+b}{ab^2}$

83.  $\frac{2-a^2}{a^2+a} + \frac{3a+4}{3a+3}$

**Complex Fractions.**

Eliminate complex fractions by multiplying the numerator and denominator by the LCD of each of the small fractions. Then simplify as you did above

EX:

$$\frac{1 + \frac{1}{a}}{\frac{2}{a^2} - 1}$$

*Find LCD :  $a^2$*

$$= \frac{\left(1 + \frac{1}{a}\right) \cdot a^2}{\left(\frac{2}{a^2} - 1\right) \cdot a^2}$$

*Multiply top and bottom by LCD.*

$$= \frac{a^2 + a}{2 - a^2}$$

*Factor and simplify if possible.*

$$= \frac{a(a+1)}{2 - a^2}$$

$$84. \frac{1 - \frac{1}{2}}{2 + \frac{1}{4}}$$

$$85. \frac{1 + \frac{1}{z}}{z + 1}$$

$$86. \frac{5 + \frac{1}{m} - \frac{6}{m^2}}{\frac{2}{m} - \frac{2}{m^2}}$$

$$87. \frac{2 + \frac{1}{x} - \frac{1}{x^2}}{1 + \frac{4}{x} + \frac{3}{x^2}}$$



### **Solving Rational Equations:**

Multiply each term by the LCD of all the fractions. This should eliminate all of your fractions. Then solve the equation as usual.

$$\frac{5}{x+2} + \frac{1}{x} = \frac{5}{x}$$

*Find LCD first.  $x(x+2)$*

$$x(x+2)\left(\frac{5}{x+2}\right) + x(x+2)\left(\frac{1}{x}\right) = \left(\frac{5}{x}\right)x(x+2) \quad \text{Multiply each term by the LCD.}$$

$$5x + 1(x+2) = 5(x+2) \quad \text{Simplify and solve.}$$

$$5x + x + 2 = 5x + 10$$

$$6x + 2 = 5x + 10$$

EX:  $x = 8 \Leftarrow$  Check your answer. Sometimes they do not check!

Check :

$$\frac{5}{8+2} + \frac{1}{8} = \frac{5}{8}$$

$$\frac{5}{10} + \frac{1}{8} = \frac{5}{8}$$

$$\frac{5}{8} = \frac{5}{8}$$

**Solve each equation. Check your solutions.**

88.  $\frac{12}{x} + \frac{3}{4} = \frac{3}{2}$

89.  $\frac{x+10}{x^2-2} = \frac{4}{x}$

90.  $\frac{5}{x-5} = \frac{x}{x-5} - 1$